

# Validation of H-H<sub>2</sub>O at Elevated Temperatures using Diffusion Experiments

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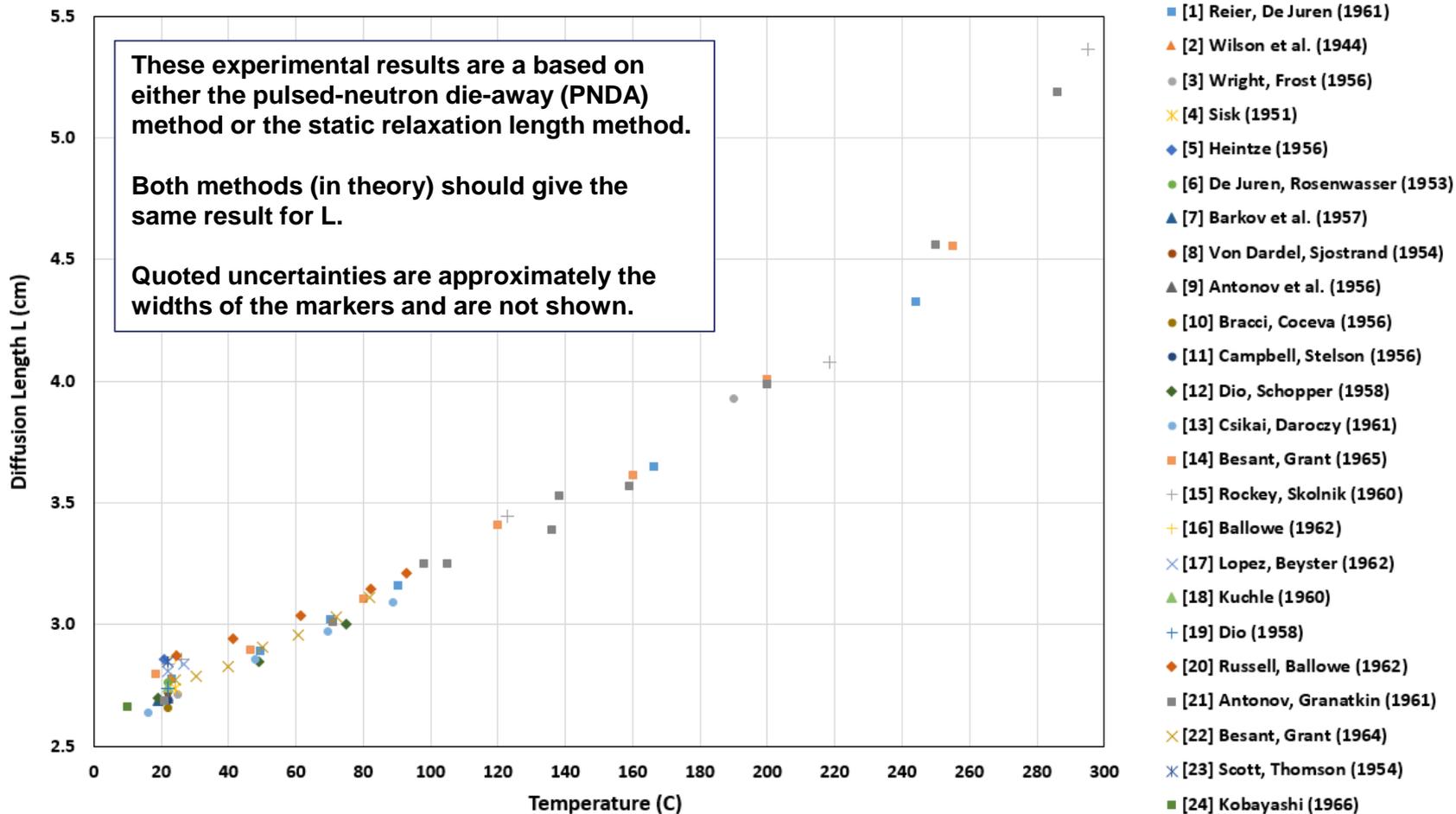
Cross Section Evaluation Working Group  
Brookhaven National Laboratory

November 4-6, 2019

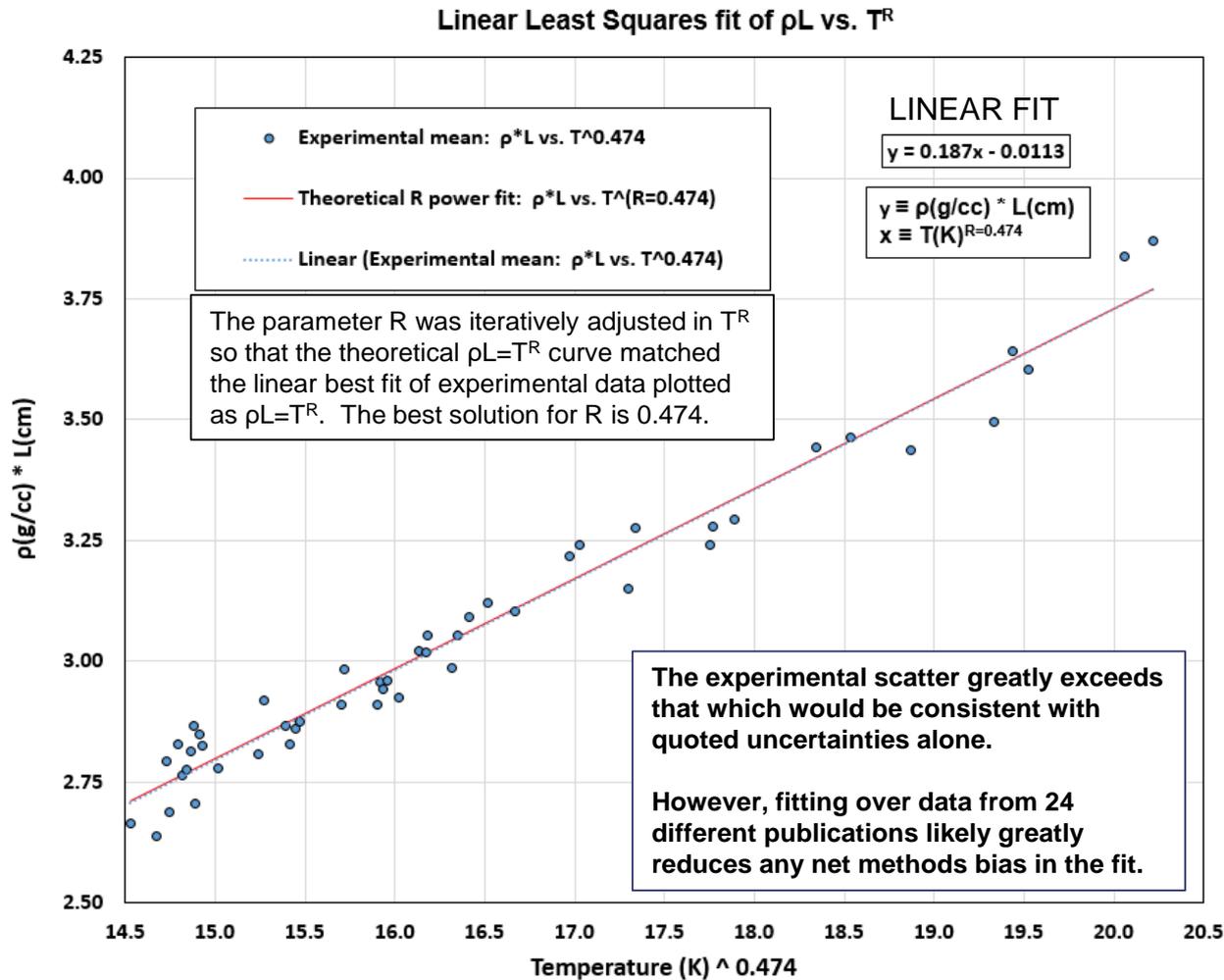
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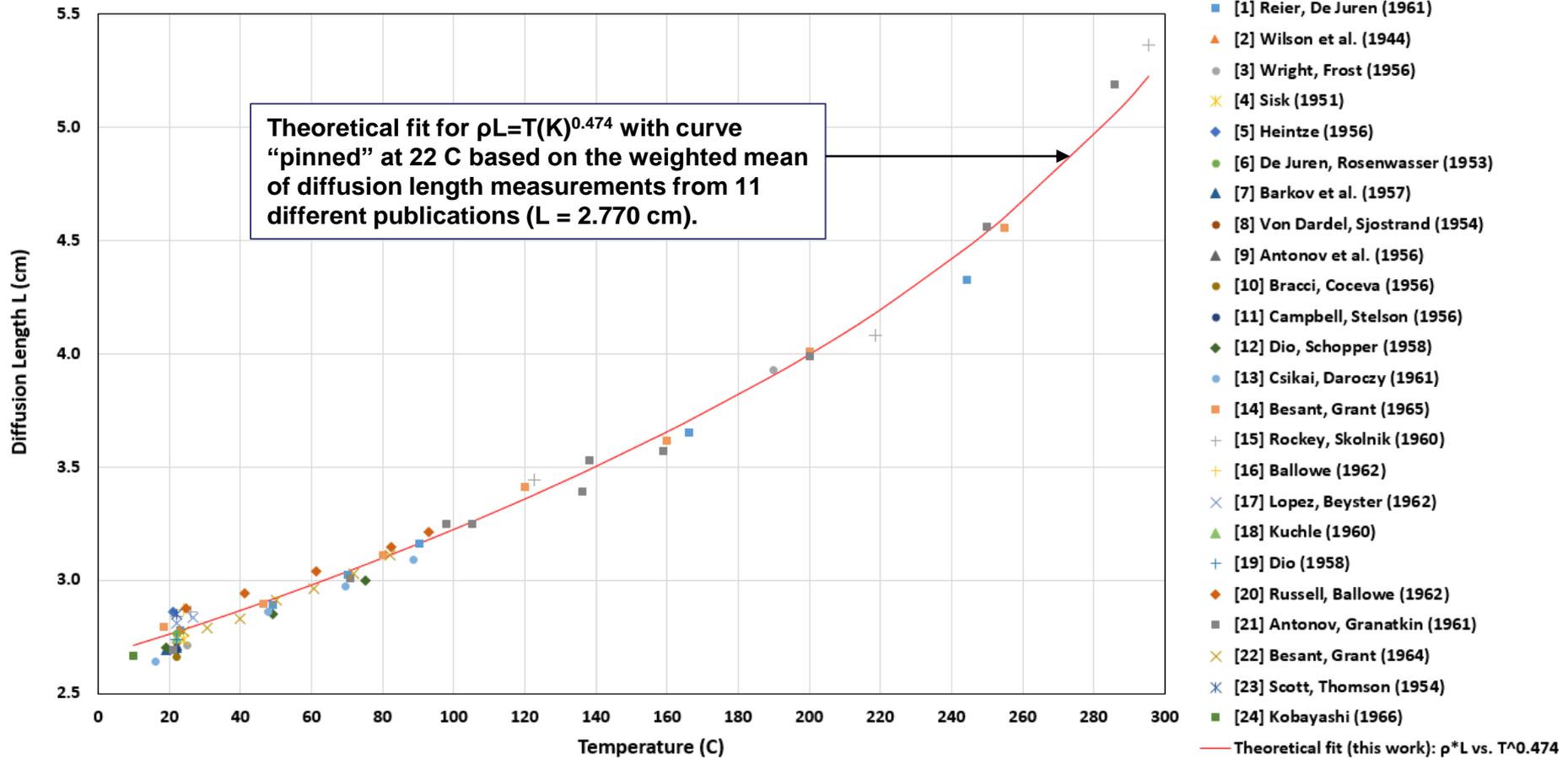
# Compilation of Historical Thermal Neutron Diffusion Length (L) Measurements for Water



# Linear and Power Fit Based on 24 Publications



# Experimental Data Compared to Power Fit

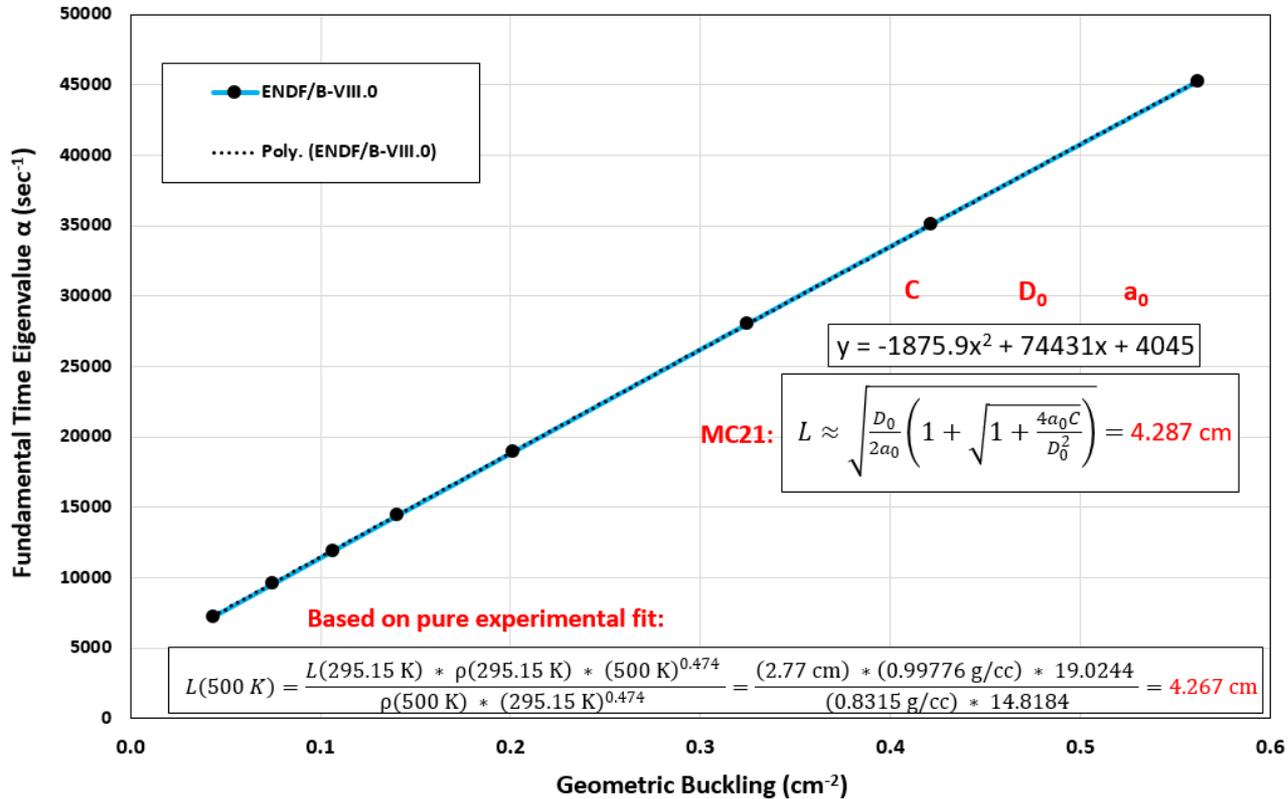


# Calculating L with MC21 PNDA Simulations

- PNDA flux decay:  $\varphi(\mathbf{r}, t) = \varphi_0(\mathbf{r})e^{-\alpha t}$ ; fundamental eigenvalue  $\alpha$  computed with MC21 simulations
- $\alpha = v\Sigma_a + vDB_g^2 - CB_g^4 + O(B_g^6) \approx a_0 + D_0x + Cx^2$  for  $x = B_g^2$
- $L \approx \sqrt{\frac{D_0}{2a_0} \left( 1 + \sqrt{1 + \frac{4a_0C}{D_0^2}} \right)} \approx \sqrt{\frac{D_0}{a_0} + \frac{C}{D_0}} \approx \sqrt{\frac{D}{\Sigma_a}}$
- Geometric buckling for spheres:  $B_g^2 = \left( \frac{\pi}{r+z} \right)^2$ .
- $z$  is approximately proportional to  $\lambda_{tr}$  and is computed at 22 C by Sjostrand (1977) for water spheres (with corrections for small geometries).
- $\lambda_{tr}$  is approximately proportional to  $D$ , and  $L \approx \sqrt{\frac{D}{\Sigma_a}}$ .
- The ratio of L at an arbitrary temperature to L at 22 C can be computed from the previously given fit.
- The expected  $D$ ,  $\lambda_{tr}$ , and  $z$  for any temperature can now be computed (accounting for density change), allowing  $B_g^2$  to be determined for water spheres of arbitrary radii and temperature.
- **Finally, calculated  $\alpha$  can be plotted vs.  $B_g^2$  for many water spheres of varying radii, and then L can be computed by solving for the coefficients  $a_0$ ,  $D_0$ , and  $C$  with a quadratic fit.**

# 500 K MC21 Calculation Compared to Prediction by Pure Experimental Fit

Calculation of Diffusion Length at 500 K



Difference between MC21 result and pure experimental fit result for 500 K is **0.5%**.  
 The uncertainty in MC21-calculated L due to ENDF uncertainty in  $\sigma_a(^1\text{H})$  is **0.9%**.

# Room Temperature and 500 K Results for Several H-H<sub>2</sub>O TSL Evaluations

